

# Grade 6 Mathematics Provincial Achievement Test

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Education

#### **Overview of Session**

- What is the purpose of the Provincial Achievement Testing Program
- How is the data from the Provincial Achievement Tests (PATs) used?
- How is the Mathematics 6 PAT designed?
- What kinds of questions will be on the Math 6 PAT?
- How did students do on the 2011 Math 6 PAT?
- What can I do to ensure my students are ready for the Math 6 PAT?
- How can I get involved in the provincial achievement test development process?



#### **Purposes of Achievement Testing Program**

- Students/parents: to provide feedback on how well the students have understood the learning outcomes from the Alberta K-6 Mathematics Program of Studies with Achievement Indicators (2007).
- **Teachers:** to provide information on how well their classes have achieved, permit comparison of their assessment information to these test results, and provide some feedback on instructional practice.



- Principals: to provide information on school achievement patterns in relation to provincial results and other information on achievement for reporting the school's annual results and for program planning and future goal setting.
- Superintendents/trustees: to provide information regarding jurisdiction results in relation to targets and provincial results for the jurisdiction 3 year education plan.



Alberta Education and Government: to provide information for monitoring student learning of selected curricular knowledge and skills in relation to provincial targets and to identify areas for improvement through curriculum redesign or program initiatives.



# How is the data from the Provincial Achievement Tests used?





#### Information for students and their parents:

- ✓ Individual Student Profiles(ISPs).
- ✓ One copy is placed in each student's cumulative file and one copy of the ISP is sent to each student's parent(s).

PAT information video for parents:

http://education.alberta.ca/parents/resources/exams.aspx



#### Information for teachers:

- ✓ Provides information on how well students have performed in relation to specific outcomes from the program of studies.
- ✓ Provides an opportunity to compare classroom/school assessment data to provincial data.



#### Information for principals:

- ✓ Provides information on school achievement patterns in relation to provincial results.
- ✓ Provides information on achievement for reporting the school's annual results.
- ✓ Provides information to assist with program planning and future goal setting.



#### Information for Superintendents/trustees:

- ✓ Provides information regarding jurisdiction results in relation to their achievement targets (the percentage of students they expect to achieve acceptable and excellent standards).
- ✓ Provides provincial results for the jurisdiction 3 year education plan.



### Information for Alberta Education and Government:

- ✓ Provides information for monitoring student learning of selected curricular knowledge and skills in relation to provincial targets (business plan).
- ✓ Helps to identify areas for improvement through curriculum redesign or program initiatives.
- ✓ part of the Accountability Pillar report.



#### Transparency is Essential to Improvement

"...there is no way that continuous improvement can occur without constant transparency fueled by good data."

Michael Fullan



# How are the Mathematics Achievement Tests designed?





#### **Overview of the Test Design Process**





#### The Test Specifications of the Mathematics 6 PAT

The information in the "front matter" of the curriculum and the content of the Specific Outcomes were both considered as the test blueprint was being developed.

#### Teachers determined the weighting of the test according to:

- Strand (N; PR; SS; SP)
- 2. Item complexity
- 3. Item format (# of MC and NR items)
- 4. Specific outcome representation



### Specific Teacher Involvement in the creation of the Test Specifications for the Mathematics 6 PAT

- July of 2009: test-blueprinting session resulting in the blueprint for the 2010 Math Pilots. One of the results was the introduction of 10 NR items at grade 6.
- July of 2011: teachers went through the same process which created a slight change to the test blueprint. (Incidentally, teachers recommended the inclusion of even more NR items.)
- July/August of 2011: the standards (cut-scores) were set.
- July/August of 2012: teachers will set the standards for the 2012 test.



#### **Blueprint for the Grade 6 Mathematics Achievement Test (Revised for 2011)**

Multiple	Multiple Choice (MC) and Numerical Response (NR)										
Item Type	Number of Items	Number of Marks	Percentage of Test								
MC	40	40	80%								
NR	10	10	20%								
Total	50	50	100%								

Content Domain of Test								
Strand Percentage of Items on Test								
Number	30 – 40%							
Patterns and Relations	20 – 30%							
Shape and Space	20 – 30%							
Statistics and Probability	10 – 20%							

Cognitive Domain of Test								
Complexity Level	Percentage of Items on Test							
Low	30 – 40%							
Moderate	40 – 50%							
High	15 – 25%							



### What kinds of questions will be on the PAT?





#### **General Characteristics of PAT Questions:**

- 1. Reflect the intent and direction given in the front matter.
- 2. Assess one or more strands and/or specific outcomes.
- 3. Are at an appropriate reading level.
- 4. Use a context applicable to students.
- 5. Meet the criteria for an effectively constructed multiple choice question.
- 7. Are statistically valid.

(Difficulty between .300 and .900, CRPB that is positive)



#### **Research regarding Multiple Choice Questions**

"Test developers need not apologize for using multiple-choice formats on achievement tests; there is strong research evidence demonstrating the high positive correlation between constructed-response and selected-response item scores for measuring knowledge and many other cognitive skills." (Rodriguez, 2003)



Item	Key	Level of Complexity	Strand	Item Descriptor	Diff.	CRPB
1011_11	В	M	N.9.1	Add three-digit numbers that are represented pictorially with base-ten blocks. (Also N.5)	.500	.336

### This item meets all the major standards

MC Item #11	GROUP N NR NF	OMIT A	В*	С	D
Dif: 0.500	Total:442 14 0	14 0.118	0.500	0.219	0.131
Rpb: 0.402	High:119 2	0.034	0.824	0.042	0.084
Crpb:0.336	Mid: 193 7	0.114	0.446	0.249	0.155
95% Con:	Low: 130 5	0.200	0.285	0.338	0.138
	Test Score Means:	16.192	22.452	16.526	18.569
Rbis: 0.502					
Crbis: 0.420	Discriminating Power:	-0.166	-0.539	-0.296	-0.054
Iri: 0.201	Standard Error of D.P.:	0.005	0.000	0.006	0.005



#### **Low-Complexity Questions**

These questions typically require students to recall and/or recognize basic mathematical concepts and procedures. Students are not expected to come up with original methods for finding a particular solution.



#### Low-complexity questions require students to:

- Recall a basic fact, term or definition
- Perform a specific procedure (+, -, x, ÷)
- Solve a one-step or simple two-step problem
- Identify an example of a concept
- Determine an unknown number in an equation or expression
- Draw, measure, or describe a 2-D shape or 3-D object
- Retrieve information from a graph, table, or figure



			Primary		% of Student Responses			ses
	Question	I	Outcome	Item				
Item	# on PAT	Strand	Number	Complexity	A	B*	C	D
7	28	N	3	Low	10.2	46.1	15.8	27.6

#### \* Correct response

28. Which of the following sets of numbers contains only composite numbers?

- **A.** 1, 2, 17, 29, 37
- **B.** 4, 9, 16, 21, 38
- **C.** 1, 8, 14, 25, 32
- **D.** 5, 11, 19, 23, 41

To answer this item correctly, students had to recall the concept of composite numbers, and apply their understanding of factors, to determine the sets of numbers that contained only composite numbers.

The most common incorrect response (D) suggests that students were unable to recall the meaning of composite numbers and instead chose the set of numbers that contained only prime numbers. The next most common incorrect response (C) suggests that students considered 1 to be a composite number.

#### **Moderate-Complexity Questions**

These questions typically involve more flexibility of thinking than those in the low-complexity category. They require a response that goes beyond the habitual and may involve more than a single step. The student is expected to decide what to do, to use reasoning and problemsolving strategies, and to bring together their skills and knowledge in order to find a solution.



#### Moderate-complexity questions require students to:

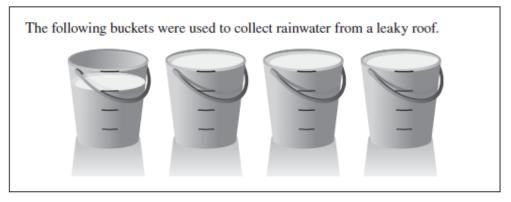
- Solve a word problem requiring multiple steps
- Compare patterns, data, or equations
- Provide or recognize justification for a solution process
- Interpret a concrete, pictorial, or symbolic representation
- Retrieve information from a graph and use it when solving a multistep problem
- Formulate a generalization about one or more objects or patterns



			Primary		% of Student Responses			ses
	Question		Outcome	Item				
Item	# on PAT	Strand	Number	Complexity	A*	В	C	D
3	13	N	4	Moderate	70.1	9.7	7.0	13.1

#### \* Correct response

Use the following information to answer question 13.



- 13. Which of the following improper fractions shows the amount of water that is collected?
  - A.  $\frac{15}{4}$
  - B.  $\frac{15}{3}$
  - C.  $\frac{13}{4}$
  - D.  $\frac{4}{3}$

To answer this item correctly, students had to interpret the provided diagram to create an improper fraction that represents the sum of all 4 represented fractions.

The most common incorrect response (D) suggests that some students simply do not understand the concept of improper fractions; e.g., some students may have reasoned that there are 4 buckets and only 3 of them were completely full of water.

#### **High-Complexity Questions**

These questions typically require students to engage in more abstract reasoning, planning, analysis, judgment, and creative thought.



#### High-complexity questions require students to:

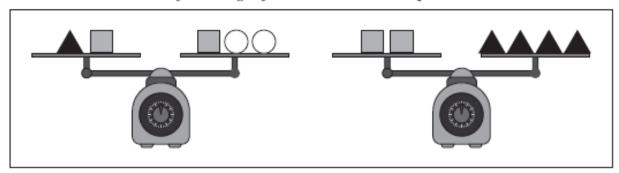
- Perform a procedure which has multiple steps and multiple decision points
- Analyze similarities and differences between procedures and concepts
- Formulate an original problem
- Solve a problem in more than one way
- Explain and justify a solution to a problem
- Describe, compare, and contrast solution processes
- Provide a mathematical justification



			Primary		% of Student Responses			
	Question	I	Outcome	Item		The contract of the contract o		ъ.
Item	# on PAT	Strand	Number	Complexity	A	B*	С	D
6	25	PR	5	High	49.2	43.0	3.9	3.6

#### \* Correct response

Use the following information to answer question 25.



- 25. How many circles does it take to balance one square?
  - A. 2
  - B. 4
  - C. 6
  - D. 8

To answer this item correctly, students had to determine the relationship between the different shapes for the balance scales to be balanced.

The most common incorrect response (A) suggests that students considered 1 square to equal 2 circles instead of 1 triangle equaling 2 circles.

### Before a question is used on a PAT the following questions must be addressed:

#### Does the question have curricular validity?

Each question must be based on the outcomes in the program of studies.

#### Does the question have instructional validity?

Questions, particularly process questions, should relate to the instructional focus as well as to the program of studies.



## How did students do on the Grade 6 2011 Mathematics Achievement Test?



Table 2.2 Standards Achieved by Students Writing the Test

Daniel Colonia	Maximum	Cut Score <sup>a</sup>		hool = 44	Province n = 36499		
Reporting Category	Possible Score	Cut Score	Number	Percent	Number	Percent	
Acceptable Standard <sup>b</sup>							
Total Test	50	23	29	65.9	29463	80.7	
Standard of Excellence							
Total Test	50	42	3	6.8	7097	19.4	
Below Acceptable Standard							
Total Test	50	N/A	15	34.1	7036	19.3	

<sup>&</sup>lt;sup>a</sup> The Cut Score is the lowest score on a test, determined by standard-setting procedures, that students must achieve for their performance to be judged "acceptable" and/or "excellent" in relation to provincial expectations.

Note: Results should be compared to your school and school authority targets.

The Acceptable Standard includes students who achieved the Standard of Excellence.

Table 4
Raw Score Results, by Reporting Category and by Gender <sup>a</sup>

		School					Province							
Reporting Category	Maximum Possible Score	All Students n = 44			Female n = 21		Male n = 23		All Students n = 36499		Female n = 17937		Male n = 18562	
		Average	S. D. <sup>b</sup>	Average	e S. D.	Average	S. D.	Average	S. D.	Average	S. D.	Average	S. D.	
Total Test	50	27.6	8.5	28.0	8.6	27.2	8.5	31.9	9.9	31.6	9.9	32.2	10.0	
Multiple Choice	40	22.4	6.8	22.6	7.2	22.3	6.6	25.9	7.8	25.6	7.7	26.1	7.9	
Numeric Response	10	5.1	2.2	5.4	2.1	4.9	2.3	6.0	2.5	5.9	2.6	6.1	2.5	
LOC - Low <sup>C</sup>	18	10.5	3.6	10.9	3.8	10.1	3.4	12.3	3.7	12.2	3.6	12.4	3.7	
LOC - Moderate	24	13.9	4.2	13.9	4.3	13.9	4.1	15.7	4.9	15.6	4.9	15.9	4.9	
LOC - High	8	3.2	1.7	3.1	1.3	3.2	2.0	3.9	2.2	3.8	2.2	4.0	2.2	
Number	17	9.3	3.4	9.2	3.7	9.3	3.2	10.6	3.8	10.5	3.8	10.7	3.8	
Patterns & Relations	14	8.4	2.3	8.7	1.9	8.1	2.6	9.2	3.1	9.2	3.1	9.3	3.1	
Shape & Space	14	7.1	2.9	7.1	3.0	7.1	2.8	9.0	3.0	9.0	2.9	9.1	3.0	
Statistics & Probability	5	2.8	1.2	2.9	1.1	2.7	1.3	3.0	1.3	2.9	1.3	3.1	1.3	

<sup>&</sup>lt;sup>a</sup> Students for whom gender information is not available are included in the "All Students" column only.

b Standard Deviation - The standard deviation is an indication of the amount of variation in a distribution. Provincially, about 68% of the students' marks will fall within plus or minus one "standard deviation" of the average mark.

<sup>&</sup>lt;sup>C</sup> Level of Complexity – Refers to the cognitive demand associated with an item: Low, Moderate, and High. Please refer to the "Mathematics 6 Subject Information Bulletin" for more information regarding item complexity.

Table 5 - 1
Results for Individual Multiple-Choice and Numeric-Response (NR) Items, by Reporting Category

Item #	% Correct Sch. Prov.	Specific Outcome	Complexity	Item Description
2	<b>56.8</b> 61.5	N.7	Low	Compare integer values represented on a number line to determine the number of points lying between two specific integer values
3	<b>29.5</b> 43.5	N.4	Low	Match a given improper fraction to a location on a number line
14	<b>77.3</b> 78.2	N.7	Low	Complete a statement demonstrating understanding of positive and negative integers in relation to zero
20	<b>77.3</b> 79.7	N.1	Low	Apply understanding of place value to match the symbolic representation of a number to its equivalent representation in word form
28	<b>38.6</b> 45.8	N.3	Low	Sort a given set of numbers into primes and composites
33	<b>40.9</b> 55.8	N.6	Low	Express a given percentage as a fraction and a decimal
1	<b>36.4</b> 39.3	N.5	Moderate	Identify the part-to-whole ratio that represents a real-life context (Gr.5, N.7)
6	<b>88.6</b> 89.0	N.7	Moderate	Determine the statement that describes the relationship between three integers
10	<b>65.9</b> 65.9	N.5	Moderate	Match a given ratio to its pictorial representation
12	<b>72.7</b> 80.5	N.3	Moderate	Identify multiples of a given number

Table 6 Results on 2010 and 2011 Items <sup>a</sup>

		2010 Achievement	Test	2011Achievement Test			
	No. of Items	School Average n = N/A	Provincial Average n = N/A	No. of Items	School Average n = N/A	Provincial Average n = N/A	
Common Items: Items appearing on both the 2010 and 2011 tests	N/A	N/A	N/A	N/A	N/A	N/A	
Unique Items: Items appearing on only the 2010 or the 2011 tests, but not on both	N/A	N/A	N/A	N/A	N/A	N/A	

<sup>&</sup>lt;sup>a</sup> This test was administered for the first time in 2011. As such, common and unique item performance reporting is not applicable.

# Performance on MC vs. NR Items (2011 Math 6 PAT)

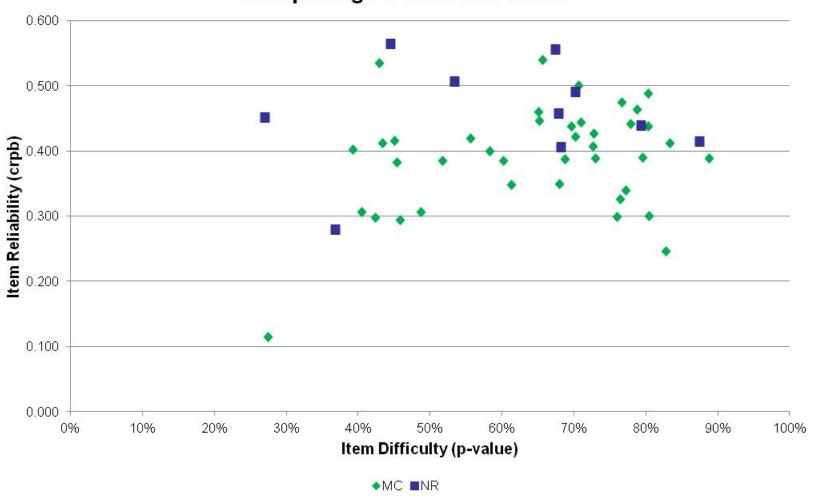
Mean on MC test items: 64.9%

Mean on NR test items: 60.7%

Mean CRPB on MC test items: 0.387

Mean CRPB on NR test items: 0.451

#### **Comparing NR and MC Items**



## What can I do to ensure that my students are ready for the PAT?





### **Balanced Assessment**

A balanced assessment approach is an integration of classroom assessments, jurisdictional assessments, and provincial assessments into a unified process that benefits instruction and student learning. (Rick Stiggins, 2008)





#### Effective instructional and assessment practices is essential

- Use formative and summative assessment practices to monitor how well your students understand the curricular outcomes.
- Provide many different types of opportunities for your students to communicate their learning.
- Make problem solving the focus of the mathematical experiences in your classroom.





#### Participate in Field Testing:

- Three unit tests in grades 6 Number, Patterns & Relations, and Shape & Space. These tests are available ONLY online, and can be administered at a time deemed appropriate by a teacher. (The same field-testing application process applies to these field tests as for all other field tests.)
- Stage 1 end-of-year field tests in both grades these are field tests comprised only of NR items (-20 items on each test). These tests are available ONLY online. (The same field-testing application process applies to these field tests as for all other field tests.)
- End-of-Year Field tests administered in May/June. These tests can be done on-line or as paper/pencil tests.



#### What's New for the Math 6 PAT?

#### **INSTRUCTION PAGES**

Can be downloaded from a link that is beside the link to the <u>Subject</u> <u>Bulletin</u> link – <u>Grade 6</u>.

#### **ANSWER SHEETS**

A sample answer sheet has been provided in the Subject Bulletin: Math 6



#### How do I find support materials for assessment?

1. Assessment Highlights

http://education.alberta.ca/admin/testing/achievement/highlights.aspx

2. Mathematics Subject Bulletin

http://education.alberta.ca/admin/testing/achievement/bulletins.aspx

3. Previously Released Examinations and Quest A+

http://education.alberta.ca/admin/testing/achievement.aspx

4. A Guide for Teachers – Grade 3 Mathematics 2010-2011

http://education.alberta.ca/admin/testing/achievement.aspx



#### Other support materials for instruction are available?

1. Mathematics Program of Studies

http://education.alberta.ca/teachers/program/math/educator/progstudy.aspx

2. Authorized Resources

http://education.alberta.ca/teachers/program/math/educator/resources.aspx

3. Support Materials

http://education.alberta.ca/teachers/program/math/educator/materials.aspx

4. FAQs for Educators

http://education.alberta.ca/teachers/program/math/educator/faq.aspx

5. Fact Sheets and Useful Links

http://education.alberta.ca/teachers/program/math/educator/links.aspx

6. LearnAlberta.ca

http://www.learnalberta.ca/Home.aspx?lang=en



# How can I get involved in the provincial achievement test development process?





#### **OPPORTUNITIES FOR INVOLVEMENT**

- 1. Classroom Field Testing
- 2. Summer Marking (ELA and FLA)
- 3. Standard Setting Working Group
- 4. Technical Advisory Groups
- 5. Item Writing Groups





## **Questions and Answers**





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